

Prediction of Non-Catalytic Esterification of Free Fatty Acids Comprising Karanja Oil Using Ann

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Abstract

The present study aims to design an Artificial Neural Network (ANN) to estimate the mole fractions resulting from the non-catalytic esterification process of Free Fatty Acids (FFA) that compose Karanja oil. The ANN was designed in the MATLAB program based on 100 pairs of data samples generated by a simulation validated in the free software DWSIM. Through a sensitivity analysis, it was determined that the inputs of the ANN were: the water mole fraction of stream 1C (1C-Xa), the oleic acid mole fraction of stream 3C (3C-Xo), the percentage conversion of the chemical reaction (%C), and the pressure drop in the reactor (-p). The methyl oleate mole fraction (9C-XM-O), methanol mole fraction (9C-Xm), triolein mole fraction (9C-XOOO), and trilinolein mole fraction (9C-XLLLL) from the liquid stream are established as outputs of the ANN. The mole fraction of methanol (10C- Xm) and the mole fraction of water (10C- Xa) from the gaseous stream. The ANN was trained and validated with a Bayesian regularization algorithm (30 hidden neurons) from which a mean squared error (MSE) = 0.00000411 and a total regression coefficient (R) of 0.99 were found. With these results and through the application of an ANOVA-type statistical analysis, it was determined with 95% reliability that the ANN has a good predictive capacity, which can be applied in the prediction of free fatty acids in the production of second-generation biodiesel (FAME).

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1. 1. Introduction

For decades, oil and non-renewable energies have been the basis of the world's energy structure; due to their high level of consumption, they have become the main driving force in both developed and developing countries. For example, according to statistics, in the European Union (EU), 30% of unprocessed energy, i.e., primary energy, is used for transportation and 98% of this depends on fossil hydrocarbons (1).

23 Luque and Melero (1) mention that EU countries have established regulations that encourage the use
24 of biofuels, and the results were significant since greenhouse gases decreased by 80% when using
25 non-edible oil residues, i.e., second-generation materials, in contrast to pollutant emissions that are
26 less than 50%, if only first generation raw materials are used. In this aspect, fatty acid metal esters
27 (FAME) become an alternative source of energy (green fuels) which are obtained from renewable
28 sources, such as the oily composition of vegetable and animal oils and fats (2). Romero (3) argues that
29 FAME is characterized by being renewable, biodegradable, and having lower toxicity than table salt;
30 its high lubricity and its intrinsically sulfur-free content, compared to diesel, favors the energy
31 efficiency of combustion and doubles the life of engines, without requiring any modification in them
32 (4). Low-sulfur diesel is usually mixed with a certain amount of FAME to improve its lubricating
33 power. In countries such as Colombia, for example, the government created Law 939 in 2004, which
34 establishes that diesel fuel must initially be of type B05, i.e., the FAME content in diesel fuel must be
35 5% (5). India has also implemented a program for large-scale production of FAME with a 20%
36 gasoline blend (6).

37 *1.1. FAME Production Processes*

38 This study will focus on producing a second-generation long-chain ester compound (C14-C24),
39 which means that it can be obtained from non-edible oils or from commercial or domestic oil residues
40 that are processed to take maximum advantage of its composition (7). In this case, the starting point
41 will be inedible oil.

42 Singh et al. (8) state that there are several methods to obtain FAME, among them thermal cracking,
43 based on any raw material of different generations. FAME has high ash and carbon residues,
44 exceeding the acceptable margin. In addition, the thermal requirement makes the process inefficient.
45 The current technology for obtaining FAME is the transesterification of non-edible vegetable oils,
46 together with alkalis, including potassium hydroxides, sodium hydroxides and compounds known as
47 alcoholates (1,9).

48 Using homogeneous alkaline catalysts involves certain drawbacks in producing FAME because it
49 cannot be reused. Ultimately, it separates into 2 phases (glycerol and soap). Therefore, it hinders the
50 purification of glycerol and decreases the yield of FAME production (10).

51 Lee et al. (11) determined that the production of FAME on an industrial scale is preferably carried out
52 from heterogeneous alkaline catalysts, especially when the oil is of high purity and contains low
53 portions of free fatty acids (FFA), due to their faster reaction speeds, about the acid catalysts.
54 Moreover, heterogeneous alkaline catalysts are ideal for synthforizing FAME concerning
55 homogeneous alkaline catalysts (8).

56 *1.2. Karanja Oil*

57 Orange oil is rich in free fatty acids (FFA), which are exploited through transesterification processes
58 by catalytic routes to produce alkyl esters (12,13). However, esterification with the influence of
59 homogeneous acid catalysts represents several disadvantages, such as corrosion of the equipment,
60 difficulties in the purification of the product and the recovery of the catalysts. To this is added the
61 high requirement of temperature and pressure in its operation (14).

62 Due to the problems presented by the use of acid catalysts, Minami and Saka (15) analyzed
63 non-catalytic supercritical conditions in the transesterification processes using supercritical methanol
64 (critical T = 239 C, critical P = 8.09 MPa), where it was evidenced that transesterification occurs from
65 the triglycerides of the oil and the FFA are simultaneously esterified. However, the operating
66 parameters exceeded the critical conditions (350 C and 20 - 50 MPa), which generates an increase in
67 operating costs and also, the product tends to degrade thermally. Therefore, according to Hussain et

68 al., esterification problems are minimized under subcritical conditions by employing non-catalytic
69 esterification techniques (13).

70 *1.3. ANNs applied in FAME procurement*

71 For the prediction of certain complex non-linear processes that cannot be described with other
72 methodologies because their results tend to be unstable, ANNs have become a tool for prediction due
73 to their high accuracy and learning capacity (16).

74 Santana et al. (17) point out that ANNs are superior to other types of modeling because they do not
75 require assumptions about the nature of a phenomenon, as with simulators. In addition, ANNs
76 recognize the mathematical procedure and achieve the learning of linear and non-linear interactions
77 between the dependent and independent variables of the proposed process from an initial experience
78 and also organize the information captured at the beginning of the training.

79 Bourquin et al. (18) recognized the advantage of using an ANN in contrast to the response surface
80 methodology (RSM) for analyzing the ejection force measurements exerted by the tablets. All
81 determined ejection properties were mainly influenced by the concentration of magnesium stearate
82 and silica aerogel, while the other factors showed much lower effects; these important relationships
83 can only be recognized from the ANN model, while the RSM model ignored them.

84 ANNs are fault-tolerant since they can continue to process information, retaining certain parts of the
85 network, even if destroyed, thanks to the redundancy of data formation. They are dynamic, and their
86 insertion is straightforward with current technology (17). They provide a better quality of adjustment
87 to the experiment due to the great flexibility caused by the various mathematical functions that this
88 non-linear modeling has (19).

89 ANNs have been used in producing FAME to such an extent that it is possible to verify its quality by
90 analyzing its chemical composition. Kinematic viscosity, for example, is a predicted property that
91 reveals the state of atomization that the fuel (FAME) will have, the fuel-air ratio and the combustion
92 efficiency. The main indicator of this property is the length of the carbon chain of FAME; as the
93 carbon chain increases, the kinematic viscosity will increase in direct proportion (20).

94 Suresh et al. developed an ANN for producing FAME using the ultrasonication time, the added CuO
95 loading and the methanol-oil molar ratio as input variables. The dependent variable was the FAME
96 yield. The optimized parameters obtained by ANN to obtain the highest FAME yield (97.82%) were
97 35 to 36 minutes in the ultrasonication stage, the catalyst loading was 2.07 wt%, and the methanol-oil
98 molar ratio resulted in 29.87:1 (21).

99 Garg & Jain (22) collected the necessary information for optimizing the process parameters of FAME
100 production from the lipid composition of algae. The production was modeled using the
101 Levenberg-Marquardt (LM) algorithm for ANN training and learning. In contrast, with the response
102 surface method (RSM), the ANN presented a better performance in predicting the results. The
103 performance parameter evaluated was the coefficient of determination (R^2), which for ANN was
104 0.999, while for RSM, it was 0.965.

105 Oladipo et al. (23) developed an ANN for producing FAME from neem oil, jatropha and used
106 cooking oils. The software used was MATLAB R2017a, and the ANN was trained with the LM
107 algorithm. The statistical performance values of the ANN were: RMSE = 0.00256 and $R^2 = 0.996$, so
108 it was established that the ANN presents a high degree of reliability in its predictions.

109 Teo SH et al. (24) evaluated and optimized the production of FAME using ANN and genetic
110 algorithms. They used crude oil from *Jatropha curcas*, a high FFA oil, which, when combined with a

111 synthesized catalyst derived from eggshell waste, resulted in the formulation of FAME with a
 112 maximum yield (98%) through glycerolysis and transesterification reactions with methanol at
 113 atmospheric pressure.

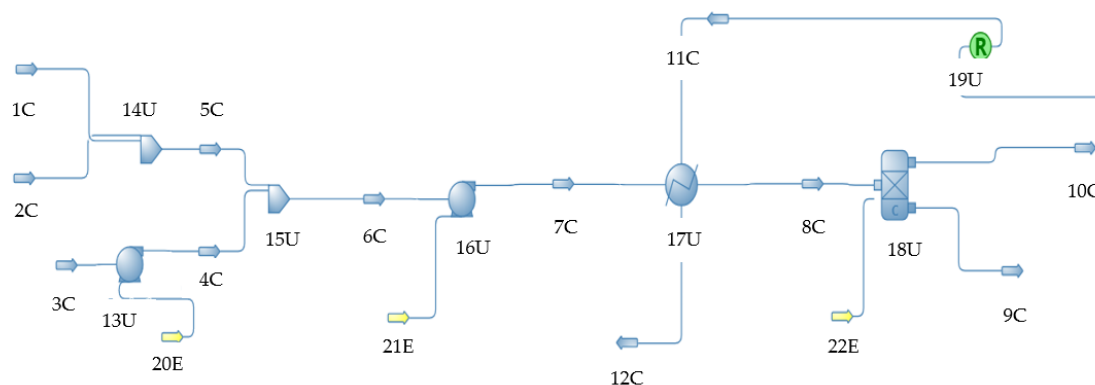
114 On the other hand, Hafidz et al. (25) employed an ANN to optimize the production of FAME from
 115 the esterification of FFA from oleic acid, catalyzed by the ionic liquid 1-butyl-3-methylimidazolium
 116 hydrogen sulfate ([BMIM] [HSO₄]) compound. As a result, FAME and O₂ conversion yield using
 117 this technique was 81.2% and 80.6%, respectively.

118 The objective of this study is to develop an ANN with the ability to predict the mole fractions of
 119 FAME from inedible oils (Karanja oil). The ANN will be developed from the simulation of the
 120 FAME production process proposed by (13), taking into account the operating conditions of the
 121 process. Future studies will be developed to incorporate the ANN into an industrial plant to optimize
 122 and continuously improve the processes.

123 2. Materials and Methods

124 *Process Description*

125 The simulation of the process corresponding to the non-catalytic esterification of FFA was carried out
 126 using the DWSIM software, taking as a reference the study developed by (13). Figure 1 describes the
 127 process used for the production of FAME.



128

129 **Figure 1.** Diagram of the non-catalytic esterification process of FFA simulated in the DWSIM
 130 program.

131 **Nomenclature:** 1C: Feed 1; 2C: Feed 2; 3C: Oil; 4C: Stream 1; 5C: Stream 2; 6C: Stream 3; 7C:
 132 Reagents 1; 8C: Reagents 2; 9C: Methyl Oleate; 10C: Methanol+Water 1; 11C: Methanol+Water 2;
 133 12C: Methanol+Water 3; 13U: Pump 1; 14U: Mixer 1; 15U: Mixer 2; 16U: Pump 2; 17U: IC (heat
 134 exchanger); 18U: Reactor; 19U: Block R; 20E: Energy B1; 21E: Energy B2; 22E: Energy R.

135 Stream 3C (1050 kg/h), consisting of oxygen (60.7%) and triglycerides (TG), is pumped
 136 (15U), which additionally receives a stream (5C), resulting from the mixing of two streams, the first
 137 containing methane mole fractions (1C) and the second consisting only of methane (2C). This
 138 mixture (7C) passes through a countercurrent heat exchanger (17U) operating at 26 kW in order to
 139 take advantage of the heat generated in the reaction (10C). After the heat exchanger, the mixture
 140 enters the conversion reactor (18U), where 99.85% O₂ conversion occurs. Table 1 details the
 141 operating parameters and compositions of the streams used in the simulation process.

142

143 **Table 1.** Parameters of process operation

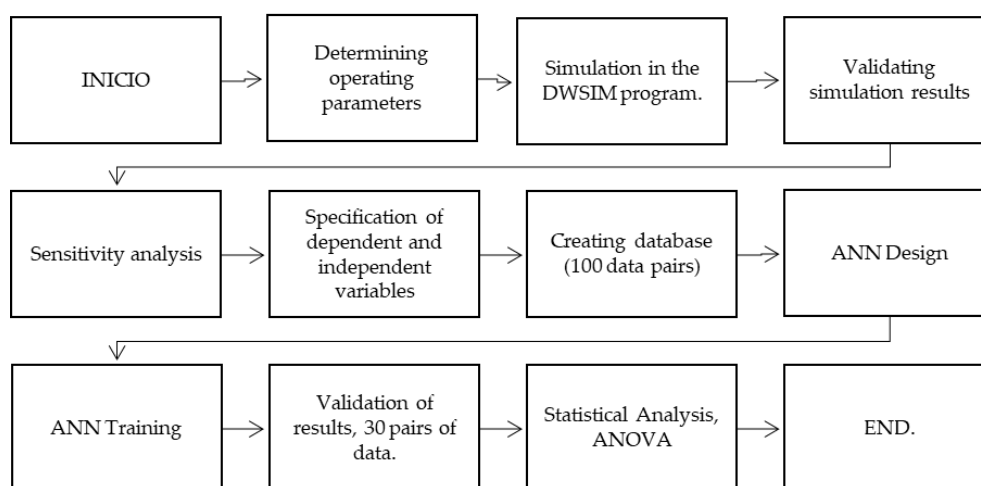
Parameters	1C	2C	3C	11C	17U	18U
<i>Pressure (bar)</i>	1	1	1		-	-
<i>Temperature (°C)</i>	64,54			220	-	-
<i>Molar flow (Kmol/s)</i>	155,33	2,81	2,02	158,03	-	-
<i>Mass flow (Kmol/s)</i>	4976,96	90,11	1050	5146,63	-	-
<i>Molar composition</i>					-	-
<i>OOO</i>	-	-	0,217	3,53E-04	-	-
<i>O</i>	-	-	0,607	0	-	-
<i>m</i>	0,99	1	-	0,99	-	-
<i>a</i>	1,13E-4	-	-	7,85E-03	-	-
<i>M-O</i>	-	-	-	1,26E-03	-	-
<i>AAA</i>	-	-	0,020	-	-	-
<i>SSS</i>	-	-	0,017	-	-	-
<i>LLL</i>	-	-	0,108	-	-	-
<i>PPP</i>	-	-	0,028	-	-	-
<i>Heat exchange area (m²)</i>	-	-	-	-	1	-
<i>Heat exchanged (kW)</i>	-	-	-	-	26	-
<i>Outlet temperature (°C)</i>	-	-	-	-	-	220
<i>Pressure drop (bar)</i>	-	-	-	-	-	-13
<i>Job (kW)</i>	-	-	-	-	-	2090,24
<i>Oleic Acid Conversion</i>	-	-	-	-	-	99,85

144 OOO: triolein, O: oleic acid, m: methanol, a: water, M-O: methyl oleate, PPP: tripalmitin, SSS:
 145 tristearin, LLL: trilinolein, AAA: triaragidine. - shows values that have been obtained thanks to the
 146 execution of the program or simply do not correspond to that section.

147 Source: (13)

148 *2.2. Methodology*

149 Figure 2 summarizes the methodological procedure used for the design of the ANN. The first step is
 150 to simulate the non-catalytic esterification process of FFA in DWSIM based on the operating
 151 parameters of Table 1, the simulation is validated, and a sensitivity analysis is performed to
 152 establish the dependent and independent variables of the process. Then, the database used for the
 153 ANN's design, training and validation is constructed. Finally, a statistical analysis is performed to
 154 determine the reliability of the prediction system of the resulting mole fractions of the FAME
 155 production process.



156

157 **Figure 2.** Methodological scheme for the design and validation of the NNA

158 *2.3. Simulation in DWSIM*

159 Santos & Van Gerven (26) consider that simulators such as Aspen Plus, Aspen Hysys, UniSim,
 160 CHEMCAD, and DWSIM, among others, are capable of modeling a plant at an industrial level and
 161 that through them, a series of physical and chemical changes can be proposed without the need to
 162 invest large amounts of money in training, configuration or optimization projects. Furthermore,
 163 Madeiros (27) states that DWSIM (CAPE-OPEN compatible) has an easy-to-use graphical interface
 164 and can simulate processes in steady or dynamic states. In addition, it allows for performing
 165 sensitivity analyses, which provide a deep understanding of the process behavior up to the point of
 166 reaching its optimal state.

167 For the simulation in DWSIM of the non-catalytic esterification process of free fatty acids that
 168 compose the Karanja oil, the operating parameters established in Table 1 were taken into account,
 169 using Raoult's Law as a thermodynamic package, which was adequately adjusted to the non-catalytic
 170 esterification process of FFA. Raoult's Law is widely used in solutions that assume ideal behavior
 171 and contain liquid and vapor phases (28).

172 *Sensitivity Analysis*

173 The following were analyzed as independent variables: the mole fraction of water in stream 1C (1C-
 174 Xa), the mole fraction of oleic acid in stream 3C (3C- Xo), the pressure drop in the reactor (-p) and the
 175 conversion percentage (%C) within the configuration of the chemical reaction, because they are those
 176 variables that exert a significant influence on the responses of the dependent variables which are: the

177 mole fractions of methyl oleate (9C-XM-O), methanol (9C-Xm), triolein (9C-Xooo) and trilinolein
 178 (9C-XLLL), this for the 9C stream. The most important mole fractions within the 10C matter line are
 179 those of methanol (10C- Xm) and water (10C- Xa).

180 Table 2 establishes the operating limits of the independent variables used as inputs to the ANN:

181

182 **Table 2.** Operating limits for ANN inputs.

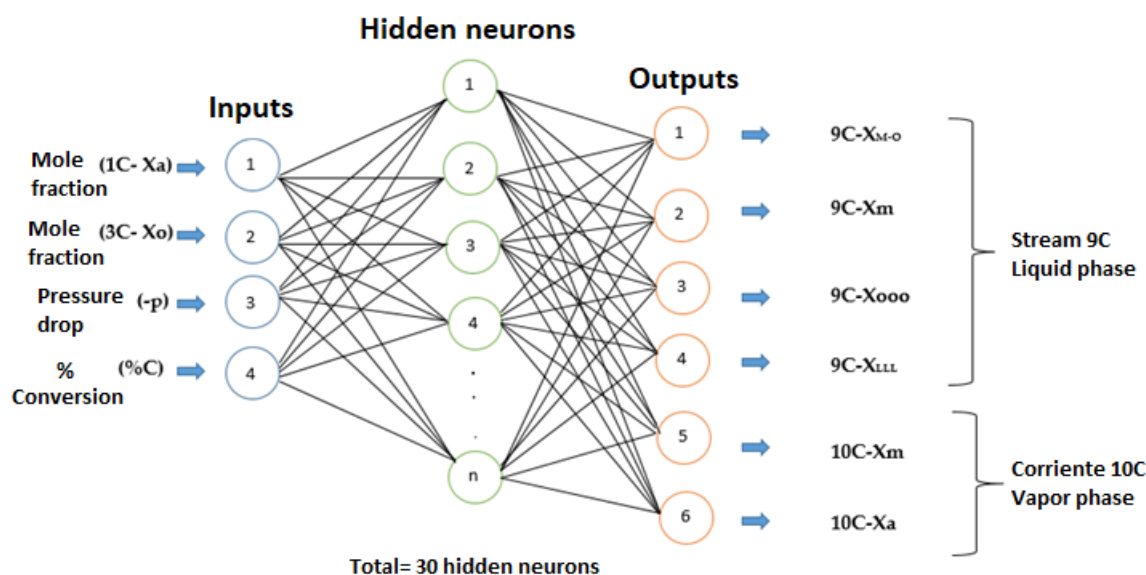
Operating Limits				
Parameter	Mole fraction a	Mole fraction O	Pressure drop (bar)	Conversion Rate (%)
Description	Current 1C	Current 3C	In the reactor	Chemical reaction properties
*Range	0 a 1	0 a 1	-1 a -35	0 a 100

183

184 2.3. Design and training of the ANN

185 Figure 3 details the design of the ANN, which was created using the MATLAB Neural Network
 186 Toolbox, version R2017b. The structure of the ANN consists of an input layer of 4 neurons
 187 corresponding to the independent variables established in the sensitivity analysis: (1C- Xa), (3C- Xo),
 188 (-p), (%C). The ANN has a hidden layer with 30 neurons and 6 neurons in the output layer, which are
 189 the dependent variables of the non-catalytic esterification process: (9C-XM-O), (9C-Xm),
 190 (9C-Xooo), (9C-XLLL), (10C- Xm), (10C- Xa).

191



192

193 **Figure 3.** Schematic of the designed ANN

194 Based on the guide proposed by Chen et al. (29), for learning, training and validation of the network,
 195 70% of the total data pairs were used, while 30% were used to perform a test to evaluate its learning
 196 level. ANN training adjusts the weights of the connections between neurons so that the ANN makes
 197 appropriate predictions for the target output data. Validation measures the ANN's prediction errors to

198 evaluate its performance. Finally, testing evaluates ANN prediction using pairs of data not used in the
199 training process (30).

200 3. Results and Discussion

201 3.1. Validation of the simulation

202 To validate the simulation performed in DWSIM, the results were compared with the work developed
203 by Hussain & Kumar (13) in AspenPlus; the outputs of the most relevant mole fractions of the 9C and
204 10C stream and the temperature of the 12C stream were taken into account. Table 3 shows the
205 comparison of the results obtained. The calculated percentage errors (%E) are below 6%, indicating
206 the reliability of the simulated process.

207

208 **Table 3.** Simulation validation

Conversion Reactor				
Currents	Mole fractions	ASPEN PLUS	DWSIM	E (%)
-13				
<i>10C</i>	X _m	0.99	0.99	0%
	X _a	7.85E-03	7.88E-03	0.38%
<i>9C</i>	X _{M-O}	0.481	0.504	4.78%
	X _m	0.17	0.16	5.88%
	X _{OOO}	0.179	0.184	2.79%
	X _{LLL}	0.103	0.097	5.82%
Heat Exchanger				
Currents	Temperature (°C)	ASPEN PLUS	DWSIM	E (%)
-13				
<i>12C</i>	Hot Fluid	210.5	209.9	0,28%

209

210 3.2. Sensitivity Analysis

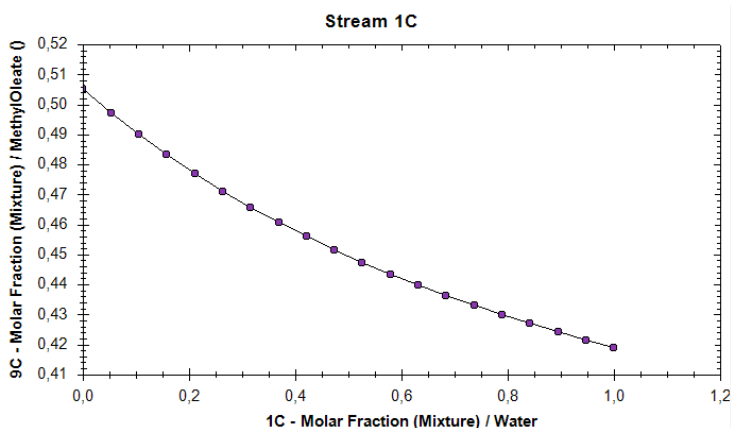
211 The sensitivity analysis enabled it to detect four independent variables that representatively affect the
212 six dependent variables. To determine the influence of the independent variables, the analysis was
213 performed on the dependent variable of greatest interest (9C-XM-O). For example, Figure 4 shows
214 the change of the variable 9C-X_{M-O} for the 1C-X_a stream (composed of water and methanol); the
215 change is inversely proportional as the amount of water in the 1C-X_a stream increases, the methanol
216 fraction decreases, and this generates that the esterification reaction is limited by the amount of
217 methanol present in the medium. On the other hand, Figure 5 shows that the dependent variable
218 9C-XM-O is directly proportional to independent 3C-X_o, because the production of FAME depends
219 on the amount of methyl oleate.

220

221 Pressure drop is also a sensitive variable to the process; as seen in Figure 6, there is an inversely
222 proportional correlation between the independent variable -p, and the dependent variable 9C-XM-O.

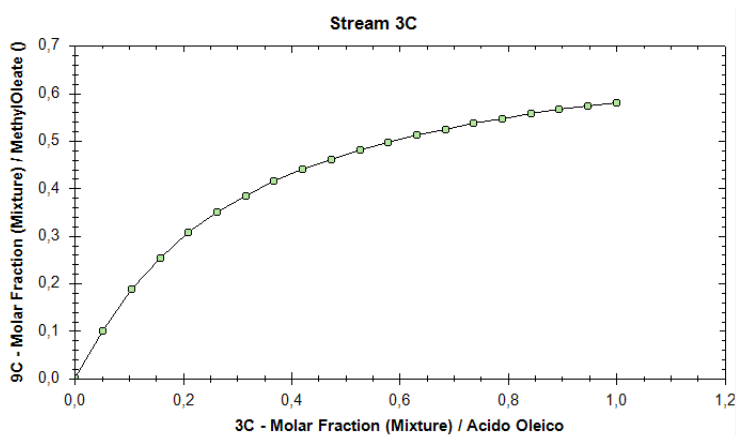
223 Using this analysis, it was possible to know the behavior of the process and to delimit the optimum
 224 pressure ranges within the conversion reactor so as not to impair the esterification. Finally, in Figure
 225 7 it can be seen that the conversion percentage strongly influences the esterification process,
 226 presenting a directly proportional relationship. As the conversion percentage increases in the reactor,
 227 the production of FAME increases.

228
229



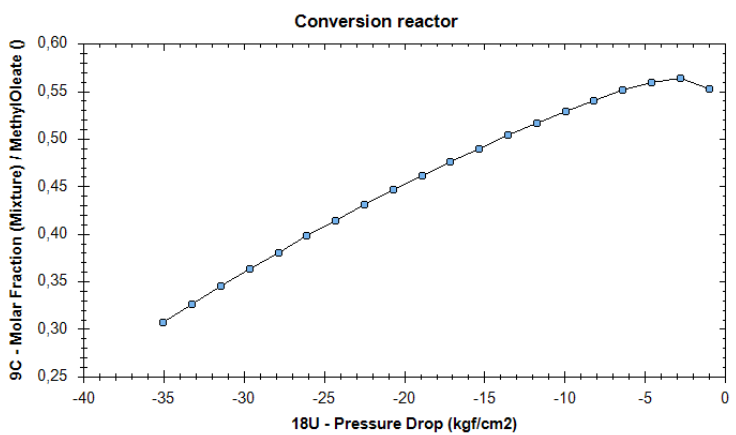
230
231

232 **Figure 4.** Impact of the variable 1C-Xa on the variable 9C-X_{M-O}



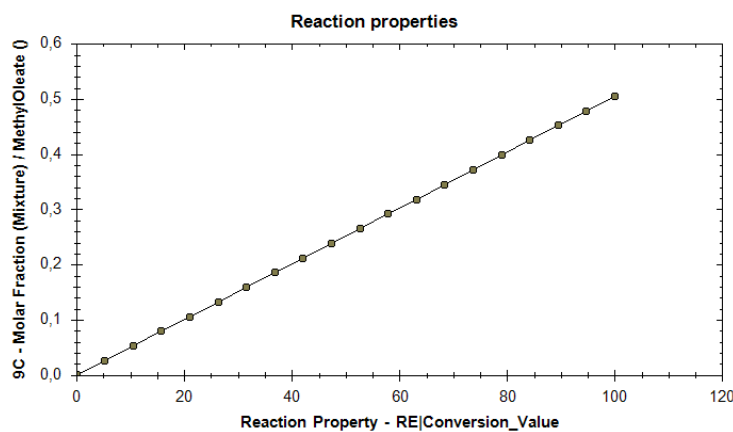
233

234 **Figure 5.** Incidence of the variable 3C- X_o on the variable 9C-X_{M-O}.



235

236 **Figure 6.** Incidence of the variable -p versus the variable 9C-X_{M-O}



237

238 **Figure 7.** Incidence of the variable %C on the variable 9C- X_{M-O} .239 **3.3. ANN topology**

240 The hidden neurons of the intermediate layer were determined through an experimental trial by
 241 varying the number of neurons and the training algorithm, evaluating the ANN performance with
 242 quantitative performance indicators (MSE and R). Table 4 summarizes the tests performed for the
 243 performance parameters. Bayesian networks (BR) discard the validation phase due to the robustness
 244 of this type of backpropagation network, which can discard the data designated for validation and
 245 take advantage of them in the relevant stages, such as training and learning. However, using the BR
 246 algorithm with 60 neurons, abnormal behavior is detected in training MSE since the error is
 247 deficient, indicating that the ANN is probably not learning but memorizing the data. In this sense, it
 248 is essential to find a balance (MSE and R values) between training and testing so that the ANN has
 249 a good prediction capacity.

250

251 **Table 4.** R and MSE values in the experimental trials.

252

Testing	Algorithm	# of neurons	Indicators	Train	Validation	Test
1	<i>LM*</i>	60	<i>MSE</i>	2,01-06	5,43E-03	1,10E-02
			<i>R</i>	0,99	9,59E-01	9,29E-01
2	<i>BR</i>	30	<i>MSE</i>	4,11*E-06	-	3,56*E-03
			<i>R</i>	9,99*E-01	-	9,76*E-01
3	<i>BR</i>	60	<i>MSE</i>	6,85E-13	-	1,76E-03
			<i>R</i>	9,99E-01	-	9,87E-01

253

254 LM: *Levenberg-Marquardt; BR: Bayesian regularization.

255

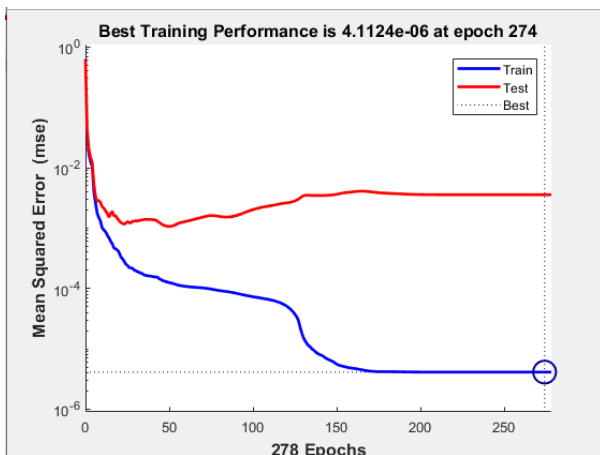
256 The training with the Bayesian Regularization (BR) algorithm is ideal for processing very noisy or
 257 complicated data; it works from the understanding of the parameters in the form of probabilities so
 258 that the weights of the network result from a set of probabilities that help to reduce prediction errors,
 259 offering an excellent generalized model (31). Furthermore, Feng et al. (32) indicate that the BR
 260 algorithm is adaptive and can identify soft or sparse forces without any initial contextualization. In
 261 addition, the BR algorithm avoids the problem of overfitting and data memorization (33).

262

263 The ANN was designed with MATLAB NNTOOL, and it is composed of three (4) input neurons, a
 264 hidden layer with 30 neurons and six (6) output neurons. According to the study developed by
 265 Abiodum et al. (34), a hidden layer may be sufficient for prediction in most ANN applications.
 266

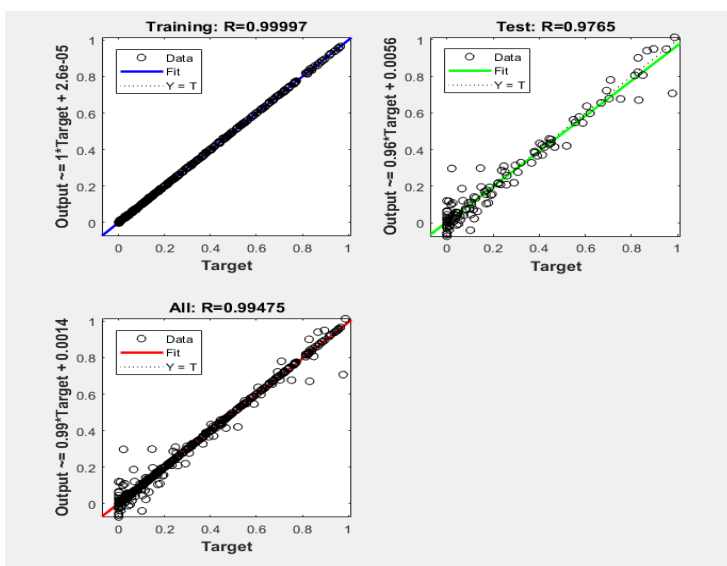
267 *3.3.1 ANN training and testing*

268 The MSE values for the training and testing phase are 4.11E-06 and 3.56E-06, respectively,
 269 indicating that the ANN performs adequately and that the predictions are made with sufficient
 270 accuracy. Figure 8 shows the mean square error (MSE) evolution during the training phase, with a
 271 final MSE of 0.0036. The MSE performance function for the training data (train) is very close to zero,
 272 indicating that the predictive capability of the network is very good.
 273



274 Figure 8. ANN training performance (MSE)
 275
 276

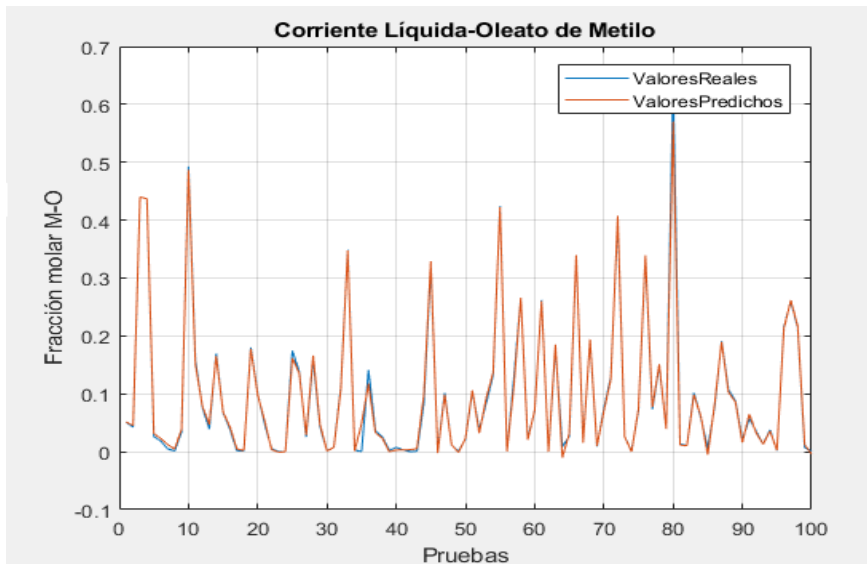
277 On the other hand, as seen in Fig.9, there is no dispersion between the outputs and targets of the ANN
 278 in both the training and test phases. The R values for the training and testing phase are 0.999 and
 279 0.976, respectively, which indicates that the outputs and targets have an acceptable correlation.
 280 Therefore, for validating the ANN, the decision was made that the R-value should be in the range of
 281 0.95 to 1 and the MSE lower than 0.025.
 282



283 Figure 9. Regression coefficient R for ANN training and testing
 284
 285

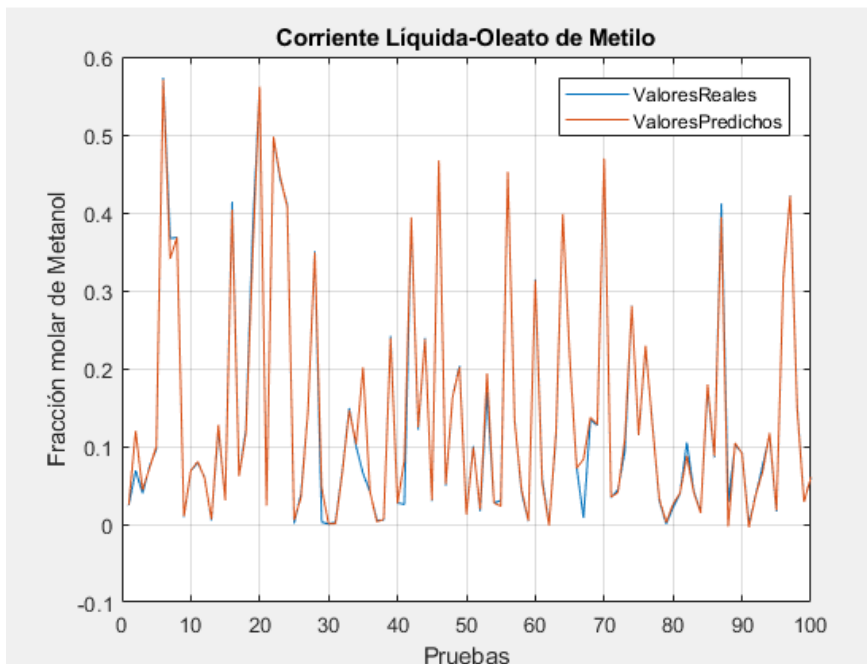
286 3.4. ANN model prediction

287 Figures 10 - 11, 12 - 13 and 14 - 15 correspond to the resulting mole fraction plots of both the liquid stream (XM-O, Xm, XOOO, XLLL) and the gaseous stream (Xm, Xa), comparing the data collected
288 from the DWSIM simulations or actual values (blue line) and the data predicted by ANN (red line).
289 Based on the observations in the figures, it can be interpreted that there is no significant difference
290 between the predicted and actual data for each of the output variables. Furthermore, the lag or
291 presence of outliers between the two curves is minimal.
292
293



294

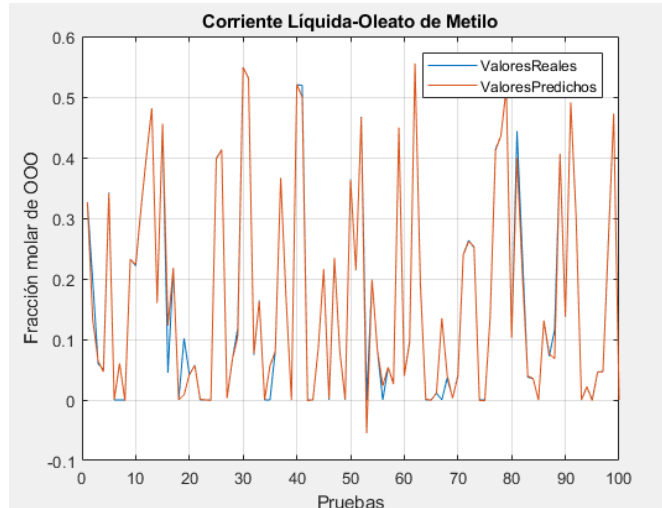
295 Figure 10. M-O mole fraction of the liquid stream, actual (DWSIM) vs. predicted (ANN)



296

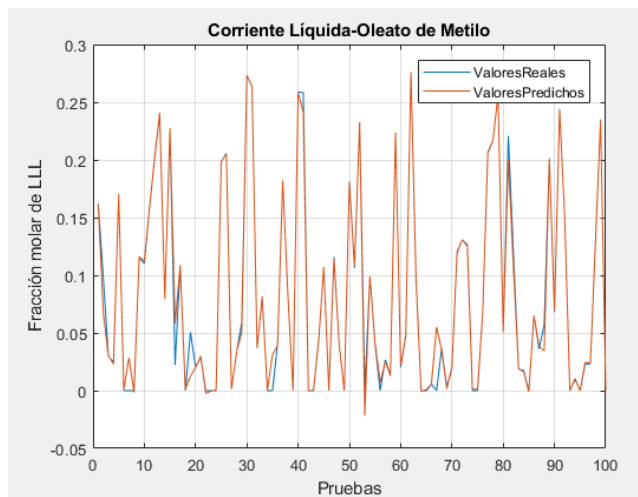
297 Figure 11. Mole fraction of m of the liquid stream, actual (DWSIM) vs. predicted (ANN)

298



299

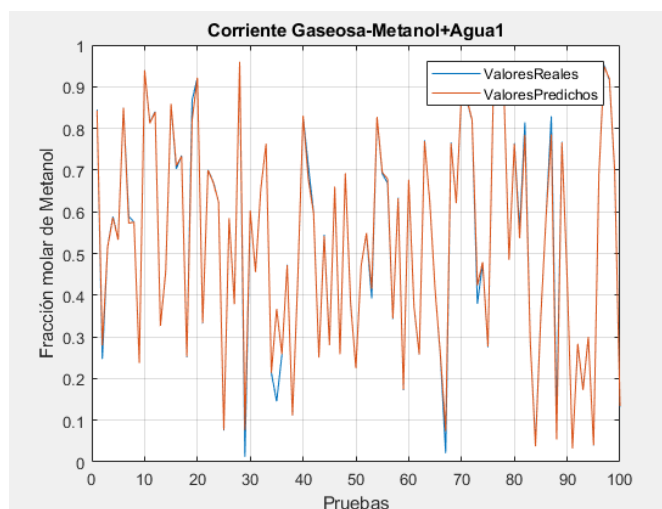
300 Figure 12. OOO mole fraction of the liquid stream, actual (DWSIM) vs. predicted (ANN)



301

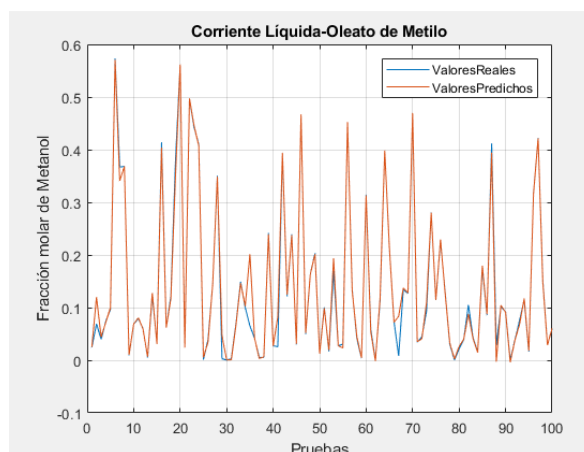
302 Figure 13. LLL mole fraction of the liquid stream, actual (DWSIM) vs. predicted (ANN)

303



304

305 Figure 14. Mole fraction of m of the gaseous stream, actual (DWSIM) vs predicted (ANN)

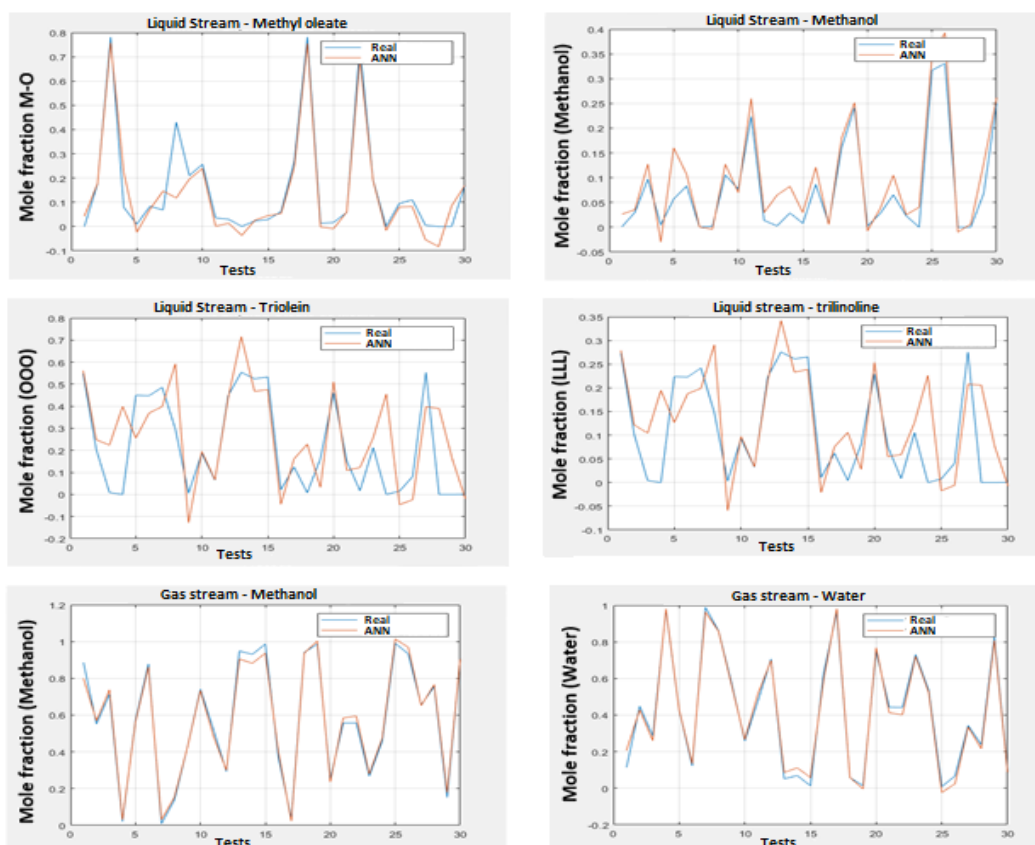


306

307 Figure 15. Water mole fraction of the gaseous stream, actual (DWSIM) vs. predicted (ANN)

308 3.5. ANN model verification

309 The ANN predictive was tested with a set of 30 random input data unknown by the ANN. The results
 310 show an overlap between the experimental data and the predictions. This indicates that ANN has an
 311 excellent predictive capacity for the dependent variables. The Figure shows the prediction of the
 312 variables under study by the ANN for the experimental data that were not considered in the network
 313 learning process.



314

315 **Figure 16.** Comparison between actual and predicted outputs of each stream. Liquid stream-9C: a)
 316 Mole fraction M-O, b) Mole fraction m, c) Mole fraction OOO, d) Mole fraction LLL. Gaseous
 317 stream-10C: a) Mole fraction m, b) Mole fraction a.

318 The research used the function ANOVA to validate the ANN statistically. Table 5 shows the
 319 results from ANOVA. For all cases, P-values (probability value in statistical significance tests) is
 320 greater than 0.05, indicating no statistically significant difference between the means of the
 321 observations and the predictions. These statistical tests reveal that the ANN constructed is statistically
 322 valid for predicting the mole fractions of methyl olein, methanol, triolein, water and trilinoline, with a
 323 confidence level of 95%.

324

325 **Table 5.** ANOVA

Source	Sum of squares	DOF	Mean square	F- value	P- value
M-O mole fraction of the 9C stream					
Inter groups	0,00386988	1	0,00386988	0,08	0,7837
Intra groups	2,9522	58	0,0509		
Total (Corr.)	2,95607	59			
Mole fraction of m of the current 9C					
Inter groups	0,00721209	1	0,00721209	0,66	0,4196
Intra groups	0,632883	58	0,0109118		
Total (Corr.)	0,640095	59			
Mole fraction of OOO of the 9C current					
Inter groups	0,0328439	1	0,0328439	0,69	0,4082
Intra groups	2,74497	58	0,0473271		
Total (Corr.)	2,77782	59			
LLL mole fraction of the current 9C					
Inter groups	0,00828621	1	0,00828621	0,72	0,3999
Intra groups	0,668125	58	0,0115194		
Total (Corr.)	0,676411	59			
Mole fraction of m of the current 10C					
Inter groups	2,61662E-7	1	2,61662E-7	0,00	0,9987
Intra groups	5,97879	58	0,103083		

Total (Corr.)	5,97879	59			
Mole fraction of a of current 10C					
Inter groups	0,0000417794	1	0,0000417794	0,00	0,9841
Intra groups	6,01191	58	0,103654		
Total (Corr.)	6,01196	59			

326

327 **4. Conclusions**

328 In this paper, an ANN capable of predicting the mole fractions derived from a non-catalytic
 329 esterification process of FFA to obtain FAME was structured, taking as a starting point a set of 130
 330 pairs of data processed in DWSIM. The ANN input variables were; the mole fraction of an of stream
 331 1C (1C- Xa), the mole fraction of O of stream 3C (3C- Xo), the percentage conversion of the chemical
 332 reaction (%C) and the pressure drop in the reactor (-p), which resulted in the prediction of 6 output
 333 variables; the mole fraction of M-O (9C-XM-O), the mole fraction of m (9C-Xm), the mole fraction
 334 of OOO (9C-XOOO) and the mole fraction of LLL (9C-XLLLL) of the liquid stream 9C, the mole
 335 fraction of m (10C-Xm) and the mole fraction of a (10C- Xa) of the gaseous stream 10C.

336

337 The network was trained with the Bayesian regularization algorithm, and its design consists of 30
 338 neurons with a running performance of $MSE = 4.11 \cdot E-06$ and $R = 0.99$. A statistical comparison
 339 analysis (ANOVA) between the experimental data (DWSIM) and the values predicted by the neural
 340 network was also used to validate the ANN. Statistical tests ($P\text{-value} > 0.05$) show that the ANN
 341 accurately predicts the mole fractions at the outputs with a 95% significance level. According to the
 342 results, this tool can be handy for large-scale FAME production, taking advantage of the FFA
 343 composition in commercial or domestic waste oils. For instance, real operating parameters of the
 344 described process must be used as input, apply them in situ and verified the predictions at the control
 345 points (outputs of the ANN).

346

347 **Supplementary Materials:** The following are available online at www.mdpi.com/xxx/s1, Figure S1:
 348 title, Table S1: title, and Video S1: title.

349

350 **Author Contributions:** Conceptualization, D.CH.V and A.S; methodology, W.D, and D.CH.V ;
 351 software, W.D, N.CH.V and J.CH.V; ANN, N.CH.V and J.CH.V; validation, D.CH.V and A.S;
 352 formal analysis, D.CH.V and C.C.T; statistical analysis, N.CH.V and J.CH.V, data curation, D.CH.V
 353 and A.S.; writing-original draft preparation, D.CH.V and A.S; writing-review and editing, D.CH.V
 354 and C.C.T; supervision, C.C.T; funding acquisition, N.CH.V, J.CH.V, D.CH.V. All authors have read
 355 and agreed to the published version of the manuscript.

356

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